distorted $\mathrm{Cd} / \mathrm{NaO}_{4}$ tetrahedron (see Table 2) considerably exceeds the predicted distance of $2.255 \AA$. The resulting 'loose' fit in this tetrahedron is reflected in the appreciably larger amplitudes of vibration of the $\mathrm{Cd} / \mathrm{Na}$ composite atom as compared with the nearly equally massive V atom: the r.m.s. amplitudes of the former are $0.153,0.141$ and $0.122 \AA$ along the crystal axes, the latter are $0.086,0.115$ and $0.088 \AA$.

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# Structure Refinement of Hafnium Phosphide, $\mathbf{H f}_{3} \mathbf{P}$ 

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Abstract. $M_{r}=566.4, \mathrm{Ti}_{3}$ P-type tetragonal structure, $P 4_{2} / n, \quad a=10.6654$ (4), $\quad c=5.2925(3) \AA, \quad U=$ $602.02 \AA^{3}, \quad Z=8, \quad D_{x}=12.49 \mathrm{Mg} \mathrm{m}^{-3}$, Мо $K \alpha, \lambda=$ $0.71069 \AA, \quad \mu=109.3 \mathrm{~mm}^{-1}$, room temperature, $F(000)=1848$. The crystal structure has been refined from visually estimated intensity data obtained from Weissenberg X-ray photographs $[R(F)=0.072$ for 341 reflections]. The atomic coordination follows rules formulated earlier for representatives of the $\mathrm{Fe}_{3} \mathrm{P}-\mathrm{Ti}_{3} \mathrm{P}-\mathrm{V}_{3} \mathrm{~S}-\mathrm{Hf}_{3}$ As family of structures.

Introduction. The atomic coordination in compounds crystallizing with the $\mathrm{Fe}_{3} \mathrm{P}-, \mathrm{Ti}_{3} \mathrm{P}-, \quad \alpha-\mathrm{V}_{3} \mathrm{~S}-$ and $\beta-\mathrm{V}_{3}$ S-type structures was thoroughly discussed by Rundqvist, Andersson \& Pramatus (1979). Some interesting coordination trends were observed, suggesting an empirical rule for the coordination of metal neighbours about the non-metal atoms. Later, the structure of $\mathrm{Hf}_{3} \mathrm{As}$ was determined by Willerström, Carlsson \& Rundqvist (1980) and classified as a new member of the $\mathrm{Fe}_{3} \mathrm{P}-\mathrm{Ti}_{3} \mathrm{P}-\mathrm{V}_{3} \mathrm{~S}$ structure family. The atomic coordination in $\mathrm{Hf}_{3}$ As was consistent with the empirical coordination rule proposed, and more recent
structure refinements of $\mathrm{Hf}_{3} \mathrm{Sb}$ and $h-\mathrm{Ta} \mathrm{a}_{3} \mathrm{Ge}$ (Willerström \& Rundqvist, 1981) and $\mathrm{Tc}_{3} \mathrm{P}$ (Rühl, Jeitschko \& Schwochau, 1982) also supported the validity of the rule. In connection with these studies it seemed worthwhile to refine the structure of $\mathrm{Hf}_{3} \mathrm{P}$. The occurrence of this compound was first reported by Ganglberger, Nowotny \& Benesovsky (1966). They found that $\mathrm{Hf}_{3} \mathrm{P}$ crystallizes with the $\mathrm{Ti}_{3} \mathrm{P}$-type structure, which was later confirmed by Lundström \& Tansuriwongs (1968). In the present work, the $\mathrm{Hf}_{3} \mathrm{P}$ structure was refined using a single crystal selected from material provided by Professor S. Rundqvist of the Inorganic Chemistry Department of Uppsala University, Sweden.

Experimental. An $\mathrm{Hf}_{3} \mathrm{P}$ powder diffraction photograph obtained using a Guinier-Hägg-type focusing camera (Philips XDC-700), $\mathrm{Cu} K \alpha_{1}$ radiation (Deslattes \& Henins, 1973), silicon SRM-640 ( $a=5.43088 \AA$ ) (Hubbard, Swanson \& Mauer, 1975) as internal calibration standard; unit-cell dimensions refined by the least-squares method, the result being in satisfactory agreement with that reported by Lundström \& Tan-
suriwongs (1968). An $\mathrm{Hf}_{3} \mathrm{P}$ single crystal in the form of a flat plate of irregular shape with approximate dimensions $0.04 \times 0.09 \times 0.02 \mathrm{~mm}$ was mounted; the $c$ axis, which was almost parallel to the long edge of the crystal, taken as the rotation axis; Weissenberg photographs ( $l=0,1,2,3$ ) recorded, Zr -filtered Mo $K \alpha$ radiation, multiple-film technique, thin silver or iron foils between successive films; intensities measured by visual comparison with an intensity scale obtained by timed exposures of one reflection from the crystal; Lorentz and polarization corrections, as well as an absorption correction using the Gaussian grid method applied; atomic scattering factors and anomalous-dispersion corrections from International Tables for $X$-ray Crystallography (1974); absorption coefficients from International Tables for X-ray Crystallography (1962), transmission factors between 0.0165 and 0.1712 . Full-matrix least-squares refinement of scale factors, one isotropic-extinction parameter, atomic positional parameters and isotropic temperature factors performed using standard crystallographic programs (Lundgren, 1976) on an IBM 370/138 computer; Cruickshank's weighting scheme (Cruickshank, Pilling, Bujosa, Lovell \& Truter, 1961), $w=1 /\left(c_{1}+\left|F_{o}\right|+c_{2}\right.$ $\times\left|F_{o}\right|^{2}$ ), applied with $c_{1}=105.86$ and $c_{2}=0.00233$; $R_{w}=0.090$;* a $\delta R$ normal probability plot (Abrahams \& Keve, 1971) was an almost straight line with a slope of 1.01 and an intercept at -0.08 ; isotropic-extinction parameter $1.6(2)$.

Discussion. The structure data obtained are given in Table 1, and the interatomic distances in Table 2.

In the structures of $\mathrm{Fe}_{3} \mathrm{P}$ - and $\mathrm{Ti}_{3} \mathrm{P}$-type compounds, the non-metal atoms are surrounded by nine nearneighbour transition-metal atoms. As first observed by Nawapong (1966) in the case of $\mathrm{Nb}_{3} \mathrm{P}$, and later by Rundqvist et al. (1979) in a further number of cases, one metal neighbour can occasionally be much more distant from the central non-metal atom than the remaining eight. For phosphides, where a fairly large number of accurate structure determinations was available, an empirical rule was found: the greater the cohesive strength of the parent metal, the smaller the coordination number for P in the corresponding phosphide (Rundqvist et al., 1979). In the series $\mathrm{V}_{3} \mathrm{P}$, $\mathrm{Nb}_{3} \mathrm{P}, \alpha-\mathrm{Ta}_{3} \mathrm{P}$ (all crystallizing with the $\mathrm{Ti}_{3} \mathrm{P}$-type structure), for instance, the ninth metal neighbour moves progressively further away from the central P atom, consistent with the increasing cohesive energy in the series $\mathrm{V}, \mathrm{Nb}, \mathrm{Ta}$.

The metal-atom coordination about P in the series $\mathrm{Ti}_{3} \mathrm{P}, \mathrm{Zr}_{3} \mathrm{P}, \mathrm{Hf}_{3} \mathrm{P}$ is illustrated histographically in Fig. 1.

[^0]Table 1. Structure data for $\mathrm{Hf}_{3} \mathrm{P}$
Space group $P 4_{2} / n$ (No. 86), origin at $\overline{1}$; all atoms in positions $8(g)$. Standard deviations are in parentheses.

|  | $x$ | $y$ | $z$ | $B\left(\AA^{2}\right)$ |
| :--- | :--- | :--- | :--- | :--- |
| $\mathrm{Hf}(1)$ | $\quad 0.1652(2)$ | $0.6422(2)$ | $0.7195(10)$ | $0.40(4)$ |
| $\mathrm{Hf}(2)$ | $0.1120(2)$ | $0.2780(2)$ | $0.5268(11)$ | $0.44(5)$ |
| $\mathrm{Hf}(3)$ | $0.0694(2)$ | $0.5343(2)$ | $0.2380(11)$ | $0.46(5)$ |
| P | $0.0426(15)$ | $0.2877(14)$ | $0.027(6)$ | $0.24(21)$ |

Table 2. Interatomic distances $(\AA)$ in $\mathrm{Hf}_{3} \mathrm{P}$
Distances shorter than $5.0 \AA$ are listed. Standard deviations are in parentheses.

| Hf(1)-2P | 2.70 (2) | $\mathrm{Hf}(3)-1 \mathrm{P}$ | 2.65 (2) |
| :---: | :---: | :---: | :---: |
| $-1 \mathrm{Hf}(1)$ | 2.926 (4) | $-1 P$ | 2.76 (2) |
| $-1 \mathrm{Hf}(3)$ | 2.977 (7) | -1P | 2.87 (2) |
| $-1 \mathrm{Hf}(3)$ | $3 \cdot 139$ (3) | $-1 \mathrm{Hf}(1)$ | 2.977 (7) |
| $-1 \mathrm{Hf}(3)$ | $3 \cdot 146$ (7) | $-1 \mathrm{Hf}(3)$ | 3.012 (10) |
| $-1 \mathrm{Hf}(2)$ | $3 \cdot 256$ (4) | -1Hf(2) | 3.050 (4) |
| $-1 \mathrm{Hf}(3)$ | 3.299 (3) | $-1 \mathrm{Hf}(2)$ | 3.058 (5) |
| $-1 \mathrm{Hf}(2)$ | 3.341 (4) | $-1 \mathrm{Hf}(1)$ | 3.139 (3) |
| -4Hf(1) | 3.359 (2) | $-1 \mathrm{Hf}(1)$ | 3.146 (7) |
| $-1 \mathrm{Hf}(3)$ | $3 \cdot 379$ (3) | -1Hf(2) | $3 \cdot 165$ (5) |
| $-1 \mathrm{Hf}(2)$ | 4.056 (4) | $-1 \mathrm{Hf}(3)$ | $3 \cdot 228$ (10) |
| -1P | 4.32 (2) | $-1 \mathrm{Hf}(1)$ | 3.299 (3) |
| $-1 P$ | 4.49 (2) | $-1 \mathrm{Hf}(1)$ | 3.379 (3) |
| $-1 P$ | 4.52 (2) | $-1 \mathrm{Hf}(2)$ | 3.958 (4) |
| -1P | 4.59 (3) | $-1 P$ | $4 \cdot 11$ (2) |
| -1P | 4.64 (3) | $-1 \mathrm{P}$ | 4.49 (3) |
| $-1 \mathrm{Hf}(2)$ | 4.939 (7) | $-1 \mathrm{Hf}(2)$ | 4.674 (7) |
| Hf(2)-1P | 2.69 (2) | -1P | 4.74 (3) |
| $-1 P$ | 2.74 (2) | $-1 \mathrm{Hf}(2)$ | 4.746 (7) |
| -2P | 2.75 (3) | $-1 \mathrm{Hf}(2)$ | 4.913 (7) 4.94 (3) |
| $-1 \mathrm{Hf}(2)$ | 3.004 (4) | $-1 \mathrm{Hf}(2)$ | 4.990 (4) |
| $-1 \mathrm{Hf}(3)$ | 3.050 (4) | $-1 \mathrm{Hf}(2)$ | 4.998 (4) |
| $-1 \mathrm{Hf}(3)$ | 3.058 (5) | -17(2) |  |
| $-1 \mathrm{Hf}(3)$ | $3 \cdot 165$ (5) | P-1Hf(3) | $2 \cdot 65$ (2) |
| $-2 \mathrm{Hf}(2)$ | $3 \cdot 177$ (9) | $-1 \mathrm{Hf}(2)$ | 2.69 (2) |
| $-1 \mathrm{Hf}(1)$ | $3 \cdot 256$ (4) | $-2 \mathrm{Hf}(1)$ | 2.70 (2) |
| $-1 \mathrm{Hf}(1)$ | 3.341 (4) | $-1 \mathrm{Hf}(2)$ | 2.74 (2) |
| $-2 \mathrm{Hf}(2)$ | 3.619 (10) | $-2 \mathrm{Hf}(2)$ | 2.75 (3) |
| $-1 \mathrm{Hf}(3)$ | 3.958 (4) | $-1 \mathrm{Hf}(3)$ | 2.76 (2) |
| $-1 \mathrm{Hf}(1)$ | 4.056 (4) | $-1 \mathrm{Hf}(3)$ | 2.87 (2) |
| -2P | 4.59 (2) | -2P | 3.96 (4) |
| $-1 \mathrm{Hf}(3)$ | 4.674 (7) | $-1 \mathrm{Hf}(3)$ | 4.11 (2) |
| $-1 \mathrm{Hf}(3)$ | 4.746 (7) | $-1 \mathrm{Hf}(1)$ | 4.32 (2) |
| -1P | 4.86 (2) | -2P | 4.33 (5) |
| $-1 \mathrm{Hf}(3)$ | 4.913 (7) | $-1 \mathrm{Hf}(3)$ | 4.49 (3) |
| $-1 \mathrm{Hf}(1)$ | 4.939 (7) | $-1 \mathrm{Hf}(1)$ | 4.49 (2) |
| $-1 \mathrm{Hf}(3)$ | 4.990 (4) | -1P | 4.50 (3) |
| -1Hf(3) | 4.998 (4) | -1Hf(1) | 4.52 (2) |
|  |  | -2Hf(2) | 4.59 (2) |
|  |  | $-1 \mathrm{Hf}(1)$ | 4.59 (3) |
|  |  | -1P | 4.63 (3) |
|  |  | $-1 \mathrm{Hf}(1)$ | 4.64 (3) |
|  |  | $-1 \mathrm{Hf}(3)$ | 4.74 (3) |
|  |  | -1Hf(2) | 4.86 (2) |
|  |  | $-1 \mathrm{Hf}(3)$ | 4.94 (3) |

The histograms indicate the number of metal-phosphorus distances within given intervals of $D / d$, where $D$ is the sum of the Goldschmidt radius for 12-coordination for the transition-metal atoms (1.45, 1.60 and $1.58 \AA$, respectively, for $\mathrm{Ti}, \mathrm{Zr}$ and Hf ) and the covalent radius for $\mathrm{P}(1 \cdot 10 \AA)$, and $d$ is the distance from the central P atom to a metal neighbour.
It is evident from the histograms in Fig. 1 that the $P$ coordination exhibits the same trend as in the series $\mathrm{V}_{3} \mathrm{P}, \mathrm{Nb}_{3} \mathrm{P}, \alpha-\mathrm{Ta}_{3} \mathrm{P}$ (compare Fig. 2 of Rundquist et


Fig. 1. Histographic representation of the coordination of metal (Hf, $\mathrm{Zr}, \mathrm{Ti}$ ) atoms about the P atoms in the structures of $\mathrm{Hf}_{3} \mathrm{P}, \mathrm{Zr}_{3} \mathrm{P}$, and $\mathrm{Ti}_{3} \mathrm{P}$. Each square corresponds to one interatomic distance. $D$ is the sum of the Goldschmidt radius for the metal atom and the covalent radius for the $P$ atom, and $d$ is the metal-phosphorus interatomic distance.
al., 1979). The tendency towards eight-coordination is more pronounced in the latter case. This is again in agreement with the empirical rule, since the cohesive energies of the V -group metals are larger than those of the corresponding metals in the Ti group.

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# Structure de l'Hydroxyborate de Thallium Hydraté, $\mathrm{TII}^{\prime}\left[\mathrm{B}_{3} \mathrm{O}_{4}(\mathbf{O H})_{2}\right], 0,5 \mathrm{H}_{2} \mathrm{O}$ 

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Abstract. $\quad M_{r}=343.8$, orthorhombic, Pnma, $a=$ 13.41 (2), $b=16.17$ (3), $c=5.43$ (1) $\AA, V=1177 \AA^{3}$, $Z=8, \quad D_{m}=3.68, \quad D_{x}=3.87 \mathrm{Mg} \mathrm{m}^{-3}, \quad$ Мо $K \alpha, \quad \lambda=$ $0.71069 \AA, \mu=275 \mathrm{~cm}^{-1}, F(000)=1208, T=293 \mathrm{~K}$, $R_{w}=0.055$ for 1154 independent reflexions. The structure contains a $\left[\mathrm{B}_{3} \mathrm{O}_{4}(\mathrm{OH})_{2}\right]^{-}$unit formed by one

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tetrahedron and two triangles. These units are linked together to form an infinite $\left[\mathrm{B}_{3} \mathrm{O}_{4}(\mathrm{OH})_{2}\right]_{n}^{n-}$ chain twisted around and along the $2_{1}$ axes; between these chains linked by hydrogen bonds, $\mathrm{Tl}^{+}$and $\mathrm{H}_{2} \mathrm{O}$ are localized. Dehydration occurs in two steps and leads to an amorphous phase; annealing gives crystalline (c) 1983 International Union of Crystallography


[^0]:    * A list of structure factors has been deposited with the British Library Lending Division as Supplementary Publication No. SUP 38413 ( 4 pp.). Copies may be obtained through The Executive Secretary, International Union of Crystallography, 5 Abbey Square, Chester CHl 2HU, England.

